Trusted Spanning Trees for Delay Tolerant Mobile Ad Hoc Networks

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Abstract—Delay Tolerant Networks (DTNs) are an extension of Mobile Ad-Hoc Networks (MANETs). Global knowledge in DTNs cannot be obtained or guaranteed due to their dynamicity, decentralized nature and non-permanent structure. Managing such networks optimally is very difficult, if not impossible. Trust management in such networks receives much attention recently due to their potential application. One solution for managing information within DTNs lies in constructing and maintaining spanning forests. DA-GRS is a local computation based model for the description of decentralized algorithms designed for dynamically distributed environments like Delay-Tolerant MANETs (DTMs). DA-GRS proposes a framework for constructing and maintaining a spanning forest in such an environment. This work introduces the notion of trust into DA-GRS resulting in T-DA-GRS algorithm. Three cost functions are suggested as means to assess robustness of trusted spanning trees. T-DA-GRS is also further improved by incorporating greedy algorithm to become T-GDA-GRS. These algorithms were tested with four different networks generated by a DTM simulator known as Madhoc. Efficiency of these algorithms is compared with optimal values.

I. INTRODUCTION

Delay Tolerant Mobile Ad Hoc Networks (DTMs) are fluctuating networks populated by a set of moving materials equipped with wireless communicating devices. These materials are called stations, nodes or devices. They can spontaneously interconnect each other without any pre-existing infrastructure [1]. What makes the management of such network difficult is their nature. DTMs are mobile, ad hoc configuring, and frequently partitioned. At a given moment, two stations belonging to distinct partitions can neither communicate directly nor indirectly (using multi-hop communications).

The most popular wireless networking technologies available nowadays for building MANETs are Bluetooth and IEEE802.11 (WiFi). This implies that devices communicate within a limited range, and stations may move while communicating. A consequence of mobility is that the topology of such networks may change quickly and unpredictably. This dynamical characteristic constitutes one of the main obstacles for performing efficient communications. Furthermore, acquiring global information in this kind of network is difficult and impractical if not impossible. Therefore management information within this network needs to be done locally, but yet effective globally. Then, algorithms designed for DTMs have to be decentralized and robust to cope with both, the dynamic and the partitioned nature of the environment.

Dynamicity Aware - Graph Relabeling System (DA-GRS) [2] is a local computation based model for the description of decentralized algorithms intended to operate in dynamically distributed environments like DTMs. In [3] the author presents an algorithm for constructing and maintaining a spanning forest in DTMs. Such a structure may be of valuable help for exchanging information efficiently between different stations for instance. The presented algorithm relies on the use of tokens (a token is an information agent). Each tree in a spanning forest owns one unique token that moves randomly within its own tree. When two tokens meet, they merge stored information from both token and become only one token. As the previous two tokens become one token, their corresponding spanning trees are merged to form a new (and larger) spanning tree.

The work introduces a trust management algorithm in DTMs by cooperating the notion of trust into the existing algorithm used in DA-GRS (T-DA-GRS). The efficiency is further improved by cooperating the ‘greedy algorithm’ concept to form T-GDA-GRS.

The paper is organized as follows. Section II presents a brief literature review. Section III explains the notion of trust management and the evaluation functions of trusted spanning trees. Section IV describes the key concept of the Trusted DA-GRS (T-DA-GRS) and the Greedy Trusted DA-GRS (T-GDA-GRS). Simulation of different network models are illustrated in Section V. Section VI compares and discusses their results. Finally the paper is concluded in Section VII.

II. RELATED WORK

A. Delay Tolerant Mobile Ad Hoc Networks (DTMs)

DTMs constitute an emerging subclass of mobile ad hoc networks that feature frequent and long-duration partitions [4]. In a DTM network, each station can reach a subset of the other stations using wireless communication abilities. Such communication ability is typically defined by a communication range and constrained by natural obstacles (e.g. walls, buildings, etc.).
At a given moment $t$, the communication graph, $G(t)$, of such network is a pair $(V_i(G), E_i(G))$, where $V_i(G)$ is a finite set of elements, called vertices, $E_i(G)$ is a binary relation on $V_i(G)$ - a subset of pairs of elements of $V_i(G)$. The elements of $E_i(G)$ are called edges and constitute the edge set of $G(t)$. An edge between node $x_i$ and $x_j$ indicates that, at time $t$, it is possible for $x_i$ and $x_j$ to exchange information. $G(t)$ may be partitioned into a set of $m$ subgraphs: $G(t) = \bigcup_{1 \leq m} P_i(t)$.

B. Dynamicity Aware - Graph Relabeling System (DA-GRS)

The DA-GRS model was invented as a help for design and analysis of decentralized applications and algorithms targeting dynamically distributed environments like DTMs. Normally, such applications and algorithms are often difficult to set up, describe and validate [5]. Using DA-GRS is a convenient way to design algorithms for DTMs, since its outstanding properties are localized in a dynamic working manner. In the context of the study, DA-GRS approach proposes a way of designing a decentralized algorithm for constructing and maintaining a spanning forest in DTMs, relying on a careful rule-based token management. Henceforth this concept will be referred to as 'DA-GRS' for brevity. The work in [5] described rules to handle four different scenarios, (a) tokens traversal in general case, (b) when a token meets another token, (c) partition occurs at a node which belongs to the spanning tree that possess the token, (d) partition occurs at a node which belongs to the spanning tree which does not possess the token. As DA-GRS constructs random spanning trees, quality (in term of trust) of each spanning tree ought to be assessed.

Let $\Gamma_i$ be the set of all possible spanning trees for $P_i$. DA-GRS randomly selects $\gamma_{\text{dagrs}} \in \Gamma_i$. An ideal situation is to be able to select $\gamma_{\text{optimal}} \in \Gamma_i$, or at least to select preferable $\gamma^* \in \Gamma_i$ such that $\gamma_{\text{dagrs}} \leq \gamma^* \leq \gamma_{\text{optimal}}$.

C. Trust Management

In human society, trust has become the basis of almost all activities, such as communications, work, etc. People gradually form the standard of mutual trust, and they also refer to opinions of the third-party in assessing the trust. Trust can be regarded as a criterion for making a judgment under complex social conditions and can be used to guide further actions [6]. In summary, trust can be viewed as the expectation or the belief that a party will act kindly and cooperatively with the trusting party [7]. It is no surprise that some research related to security or mutual cooperation on multi-agent system paid particular attention to trust factor in various facets, [8], [9], [10].

In early stage of trust and security on MANETs, several trust and security establishments relied on cryptographic methods, authentication codes and hashing chains for their solutions. Although these schemes are effective, they are centralized system which produced significant communication overheads from both preprocessing and during processing periods, as well as energy consuming. These approaches are also not applicable to DTMs. In the last few years, cooperation enforcement methods (avoidance the effect of selfish nodes on the networks’ robustness [11]), and reputation schemes [7], [12], [13] have been proposed for trust establishment in MANET. Recent literature suggests that the cooperation enforcement techniques are more appropriate if the primary goals are availability, robustness of the network, and the overall throughput. A comprehensive survey on cooperation enforcement can be found in [14], while detailed discussion on peer-to-peer key and trust management approach can be found in [15].

Quality of service is a key issue in DTMs where members, mobile stations may present different level of services. In [11] different strategies for mobile nodes are examined. In this work, trust is used in establishing on-the-fly security (in term of robustness) in a purely self-organized manner of DTMs (no pre-established relationship among nodes or off-line key distribution). An assumption is made that a trust model has been established and provision of trust information to different nodes is assumed.

III. TRUSTED SPANNING TREES

Trust spanning tree in this work is a spanning tree which is cooperatively built in a cluster/partition of trusted nodes in order to manage information embedded in a MANET. Trust level of a node $n$, denoted by $\text{trust}(n)$, where $\text{trust}(n) \in Z^+$, defines the level of quality of services it can provide. Whether a node $n$ can be trusted is determined by a given threshold. Let $\Theta_i = \{n' \in V_i(G) | \text{trust}(n') \leq \text{threshold}\}$ be the set of all non-trustable nodes at moment $t$. A node in a cooperative network can have low level of trust for various reasons such as low battery, poor communication signal, moving out of communication range, etc. An ideal situation is to determine an optimal trusted spanning tree among many possibilities in a given cooperative network. To date, there is no efficient algorithm which can generate an optimal spanning forest in DTMs due to their dynamic and decentralized characteristics and lack of global knowledge in the cooperative network. Nevertheless, more robust trusted spanning trees (i.e. spanning trees where less trustable nodes are leaves) are preferable to arbitrary ones. In order to determine robust trusted spanning trees, this work introduces quality measurement for trusted spanning trees by means of three cost functions.

A. Cost functions

A trusted spanning tree in this work is evaluated by three cost functions, these are $\text{weight}()$, $\text{weight\_penalty}()$ and $\text{isolating\_low\_trusted\_node}()$. In order to summarize the quality of created trust spanning tree, the value of functions from different studied algorithms will be compared where a higher value indicates a better quality. These functions will be applied to an optimal trusted spanning tree and will be used as best-case. Figure 1(a) and (b) are examples to illustrate the idea behind these cost functions which the threshold of being non-trustable node is defined as equal to one.

1) $\text{weight}()$ function: Having nodes with low trust levels localized on leaves is advantageous since they would not be responsible for forwarding information to others. Furthermore, loosing them at these positions in the trusted spanning trees
has little effect to the overall structure. On the contrary, as low trust levels have tendency to break away from the network, allowing them to have high degrees presents a difficult task of re-connecting the two trusted spanning trees as a result of their breaking away. Therefore, in order to minimize the task of re-connecting trusted spanning trees, nodes with lowest trust levels should be assigned the lowest degree position in the trees. The weight() function of a trusted spanning tree can be determined by the following equation:

$$weight(\gamma) = \sum_{x \in V(\gamma)} trust(x) \cdot degree(x)$$  \hspace{1cm} (1)$$

The function degree(x) represents the degree (or the number of edges which is member of \( \gamma \)) of node x. Figure 1 is used to illustrate how the weight function can assess this quality. In Figure 1(a), the node with lowest trust level gets the highest degree, while the node with highest level gets the lowest degree (i.e. the node A has a trust level of 1 and degree of 3, while the node E a trust level of 5 and degree of 1), hence the weight() function for this trusted spanning tree is 22. Figure 1(b) depicts the opposite (i.e. the node with highest trust level possess highest degree (node E), while the node with lowest level possess lowest degree (node E)). The weight() function for this trusted spanning tree is 34.

2) weight_penalty() function: This function is used in conjunction with the weight() function, it assigns an additional penalty to non-trustable nodes \( \Theta(\gamma) \) which are not leaves. This additional penalty can be determined by the following equation:

$$weight\_penalty(\gamma) = \left( \sum_{x \in V(\gamma)} trust(x) \cdot degree(x) \right) - \left( \sum_{n' \in \Theta(\gamma)} degree(n') - 1 \right)$$  \hspace{1cm} (2)$$

As all non-trustable nodes with degrees higher than 1 are assigned additional penalty. Therefore, the trusted spanning tree in Figure 1, (a) incurs additional penalty of 19, while the one in Figure 1, (b) does not as there is no node with lowest trust level possesses the degree of more than 1 (i.e. all nodes with trust level of 1 are at terminal).

3) isolating_low_trusted_node() function: This function indicates the efficiency of a trusted spanning tree by noting how well it can isolate non-trustable nodes. The function measures the percentile of \( n' \) nodes at terminal position. The higher value of isolating_low_trusted_node() function signifies better quality trusted spanning tree. Let \( \Theta^*(\gamma) = \{n' \in \Theta(\gamma) | n' \text{ is at terminal position of } \gamma \} \). The isolating_low_trusted_node() function can be determined by the following equation:

$$isolating\_low\_trusted\_node(\gamma) = \left( \frac{\Theta^*(\gamma)}{\Theta(\gamma)} \right) \cdot 100$$  \hspace{1cm} (3)$$

Hence, the isolating_low_trusted_node value for Figure 1(a) is 33.33% while this value is 100% for Figure 1(b).

B. Optimal tree

Assuming that every nodes x and their trust level in G are known, the optimal tree, at any particular time t, can be defined as: \( \gamma^{optimal} \in \Gamma_t, \forall \gamma \in \Gamma, weight(\gamma^{optimal}) \leq weight(\gamma) \)

IV. ALGORITHMS FOR BUILDING TRUST SPANNING TREES

Trust management within a partition of DTM is very difficult because of its dynamicity, decentralized nature and non-permanent connection that can break up into two or more partitions at any moment. Although cooperative working manner among stations (i.e. nodes) within a DTM can be assumed, any trust management algorithm has to work at local level as global knowledge of the network cannot be acquired.

Spanning tree is a structure which facilitates trust management where communication among the set of nodes in the tree is possible via its edges (i.e. communication edges). In [2], the authors introduce an algorithm to manage spanning forest within a DTM environment. It constructs possible spanning trees in a DTM by means of using tokens. Token can be seen as an information agent, initially possessed by each node, that becomes obsolete as it connects to another spanning tree. Hence, each spanning tree owns a unique token. In this work, trust level is assumed to be from 1 to 5 (1 being the lowest and vice versa).

A. T-DA-GRS

In this work, trust management in DTM is maintained by incorporating the notion of trust into the algorithm in DA-GRS. Hereafter, this algorithm will be referred to as T-DA-GRS for ease of reference. In T-DA-GRS, trusted spanning trees are initially constructed in the same way as in DA-GRS. Each token moves within their own trusted spanning tree. Merging of two trusted spanning trees occurs when two tokens meet. After the merge is complete, a new and larger trusted spanning tree is formed, and the two tokens also merge in one unique token. Figure 2, illustrates this operation. There are four trusted spanning trees and their tokens are at nodes A, B, C and D respectively. These tokens are within each others access range. T-DA-GRS merges trusted spanning trees randomly. In this example, the trusted spanning tree with token at node A happens to merges with another trusted spanning tree with token at node B. Note that no consideration is given to the trust level of each node.
B. T-GDA-GRS

Since T-DA-GRS constructs and merges trusted spanning trees randomly. Robustness of each trusted spanning tree is left to chance. Therefore, T-DA-GRS is more likely to result in trusted spanning trees with low cost function values. In order to improve the possibility of generating more robustness of spanning trees, T-GDA-GRS is further improved by incorporating greedy algorithm concept. The principle of this improvement arises from the fact that merging tokens located on highest trust level nodes is likely to result in a more robust trusted spanning tree (i.e. a trusted spanning tree with higher cost function values). Hereafter, this algorithm will be referred to as T-GDA-GRS for brevity. The extension in the merging operation in T-GDA-GRS is described below.

**Algorithm 1 Look for other trees (tokens) around token $\tau_i$**

1: $\tau_{best}$ is the most trusted token in one hop neighbourhood
2: if $\tau_{best} \neq \{\}$ then
3: $\text{Merge \_With}(\tau_i, \tau_{best})$ //merge the two tokens
4: else
5: $\text{Move \_Token}(\tau_i)$ //continue to move the token randomly
6: end if

Figure 3 illustrates this improvement. In this instance, merging of two trusted spanning trees occurs where tokens are at nodes with highest trust level resulting in a larger and more robust trusted spanning tree than in Figure 2.

V. SIMULATION OF TRUSTED SPANNING TREES IN DTMS

Classical DTM applications include Military Ad-Hoc Networks, Vehicle Ad-Hoc Network (VANETs), Exotic Media Networks, and etc. Suitable networks for simulation of any MANET ought to comprise lay-out of nodes (citizens), environmental properties and radio propagation (communication link) which reflect real-world situations. The networks used in this work were generated by Madhoc [16] (an ad-hoc networks simulator that provides mobility models allowing realistic motion of citizens in variety of environments). Simulations in this work are divided into two main categories, static and dynamic. In each category, two different characteristic networks are selected. To ensure validity of the simulation, three different networks of each characteristic are generated. Altogether, twelve networks were selected, Table I summarizes the networks and their characteristics in each category used in this work.

![Fig. 4. Summary of graphs used according to its characteristic](image)

Properties of each type of networks is discussed in the following sub-sections.

A. Static Networks

While dynamic networks are more appropriate in simulation of this type, the use of static networks was not be overlooked as they provided good starting point to investigate flaws and shortcomings of proposed algorithms. Random and city street scenarios were selected for static networks. Figures 5(a) and 5(b) depict examples of random and city street networks respectively. Tables I and II summarize properties of each networks in the static category.

![Fig. 5. Examples of Random and City Street Networks](image)

B. Dynamic Networks

The duration consists of 40 simulation steps, a simulation step was taken at 0.25 seconds interval. A duration in a
TABLE I
PROPERTIES OF RANDOM NETWORKS (STATIC)

<table>
<thead>
<tr>
<th></th>
<th>random 1</th>
<th>random 2</th>
<th>random 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>number of stations</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>average number of degrees</td>
<td>4.50</td>
<td>4.66</td>
<td>4.22</td>
</tr>
<tr>
<td>maximum number of degrees</td>
<td>10</td>
<td>15</td>
<td>10</td>
</tr>
<tr>
<td>minimum number of degrees</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>total connections</td>
<td>331</td>
<td>356</td>
<td>331</td>
</tr>
</tbody>
</table>

TABLE II
PROPERTIES OF CITY STREET NETWORKS (STATIC)

<table>
<thead>
<tr>
<th></th>
<th>street 1</th>
<th>street 2</th>
<th>street 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>number of stations</td>
<td>28.12</td>
<td>32.16</td>
<td>43.05</td>
</tr>
<tr>
<td>average number of degrees</td>
<td>7.68</td>
<td>7.68</td>
<td>7.69</td>
</tr>
<tr>
<td>average of max. number of degrees</td>
<td>13.20</td>
<td>16.10</td>
<td>14.83</td>
</tr>
<tr>
<td>average of min. number of degrees</td>
<td>2</td>
<td>1.07</td>
<td>1</td>
</tr>
<tr>
<td>average number of total connections</td>
<td>743.17</td>
<td>577.60</td>
<td>747.40</td>
</tr>
</tbody>
</table>

TABLE III
PROPERTIES OF SHOPPING MALL NETWORKS (DYNAMIC)

<table>
<thead>
<tr>
<th></th>
<th>mall 1</th>
<th>mall 2</th>
<th>mall 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>number of stations</td>
<td>99</td>
<td>99</td>
<td>99</td>
</tr>
<tr>
<td>average number of degrees</td>
<td>11.07</td>
<td>11.51</td>
<td>39.61</td>
</tr>
<tr>
<td>average of max. number of degrees</td>
<td>19.10</td>
<td>19.41</td>
<td>55.34</td>
</tr>
<tr>
<td>average of min. number of degrees</td>
<td>2.61</td>
<td>2.39</td>
<td>19.44</td>
</tr>
<tr>
<td>average number of total connections</td>
<td>433</td>
<td>448.60</td>
<td>1,547.05</td>
</tr>
</tbody>
</table>

TABLE IV
PROPERTIES OF HIGHWAY NETWORKS (DYNAMIC)

<table>
<thead>
<tr>
<th></th>
<th>highway1</th>
<th>highway2</th>
<th>highway3</th>
</tr>
</thead>
<tbody>
<tr>
<td>number of stations</td>
<td>80</td>
<td>80</td>
<td>80</td>
</tr>
<tr>
<td>avg. number of degrees</td>
<td>11.07</td>
<td>11.51</td>
<td>39.61</td>
</tr>
<tr>
<td>avg. of max. number of degrees</td>
<td>19.10</td>
<td>19.41</td>
<td>55.34</td>
</tr>
<tr>
<td>avg. of min. number of degrees</td>
<td>2.61</td>
<td>2.39</td>
<td>19.44</td>
</tr>
<tr>
<td>avg. number of total connections</td>
<td>433</td>
<td>448.60</td>
<td>1,547.05</td>
</tr>
</tbody>
</table>

A. Results from Static Networks

Tables V and VI summarize the averages for the three cost function values for the optimal trusted spanning trees and those generated by T-DA-GRS and T-GDA-GRS for random and city streets networks respectively.

TABLE V
AVERAGES OF COST FUNCTION VALUES (RANDOM NETWORKS)

<table>
<thead>
<tr>
<th></th>
<th>weight</th>
<th>weight_penalty</th>
<th>isolating_low_trusted_node</th>
</tr>
</thead>
<tbody>
<tr>
<td>Optimal Value</td>
<td>632.73</td>
<td>623.63</td>
<td>97.07</td>
</tr>
<tr>
<td>T-GDA-GRS</td>
<td>577.60</td>
<td>554.07</td>
<td>65.01</td>
</tr>
<tr>
<td>T-DA-GRS</td>
<td>518.73</td>
<td>489.13</td>
<td>48.32</td>
</tr>
</tbody>
</table>

TABLE VI
AVERAGES OF COST FUNCTION VALUES (CITY STREET NETWORKS)

<table>
<thead>
<tr>
<th></th>
<th>weight</th>
<th>weight_penalty</th>
<th>isolating_low_trusted_node</th>
</tr>
</thead>
<tbody>
<tr>
<td>Optimal Value</td>
<td>747.40</td>
<td>743.17</td>
<td>99.20</td>
</tr>
<tr>
<td>T-GDA-GRS</td>
<td>717.30</td>
<td>693.60</td>
<td>87.05</td>
</tr>
<tr>
<td>T-DA-GRS</td>
<td>546.07</td>
<td>508.07</td>
<td>49.88</td>
</tr>
</tbody>
</table>

For both static networks, T-DA-GRS achieved the average of 77.15% for weight value, 72.96% for weight_penalty value and 50.03% for isolating_low_trusted_node value of their corresponding optimal values. These values are 93.82%, 91.28% and 77.47% for T-GDA-GRS respectively. For both dynamic networks, T-DA-GRS achieved the average of 56.24% for weight value, 53.16% for weight_penalty value and 46.78% for isolating_low_trusted_node value of their corresponding optimal values. These values are 67.23%, 65.12% and 73.53% for T-GDA-GRS respectively.

B. Results from Dynamic Networks

Tables VII and VIII summarize the averages for the three cost function values for the optimal trusted spanning trees and those generated by T-DA-GRS and T-GDA-GRS for shopping mall and highway networks respectively.

C. Discussion

While both T-DA-GRS and T-GDA-GRS could not yield optimal performances, trusted spanning trees generated by both algorithms were comparable to optimal ones and ought to be simulation was set to last 10 seconds. The duration was selected carefully to reflect what may happen in practice. In reality, changes in a highway network are likely to occur more often than in a shopping mall network. Figures 6(a) and 6(b) depict initial configurations at $t_0$ of the shopping mall and highway networks respectively. Tables III and IV summarize properties of each networks in the dynamic category.

VI. SIMULATION RESULTS

As stated earlier in Section III, determination of an optimal spanning tree in MANETs is extremely difficult due to their dynamic and lack of global knowledge and no algorithm exists to date. Since the networks used in this work were generated by Madhoc, global knowledge and changes in their dynamicity could be predetermined. Therefore, optimal spanning trees can also be obtained. This advantage makes it possible for the efficiency of the two algorithms, the three cost functions proposed and robustness of spanning trees generated in this work to be evaluated. Hereafter, all values which can be predetermined from optimal spanning trees will be referred to as optimal value for ease of reference. In order to ensure validity of the study, 375 runs were carried out for each of the four networks. Their findings are discussed below:

(a) Shopping Mall. (b) Highway.

Fig. 6. Example of Shopping Mall and Highway Networks at $t_0$
TABLE VII
AVERAGES OF COST FUNCTION VALUES (SHOPPING MALL NETWORKS)

<table>
<thead>
<tr>
<th></th>
<th>weight</th>
<th>weight_penalty</th>
<th>isolating_low_trusted_node</th>
</tr>
</thead>
<tbody>
<tr>
<td>Optimal Value</td>
<td>976</td>
<td>769.03</td>
<td>97.6</td>
</tr>
<tr>
<td>T-GDA-GRS</td>
<td>643.80</td>
<td>619.97</td>
<td>75.84</td>
</tr>
<tr>
<td>T-DA-GRS</td>
<td>537.03</td>
<td>504.07</td>
<td>48.12</td>
</tr>
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TABLE VIII
AVERAGES OF COST FUNCTION VALUES (HIGHWAY NETWORKS)

<table>
<thead>
<tr>
<th></th>
<th>weight</th>
<th>weight_penalty</th>
<th>isolating_low_trusted_node</th>
</tr>
</thead>
<tbody>
<tr>
<td>Optimal Value</td>
<td>972</td>
<td>968.10</td>
<td>99.8</td>
</tr>
<tr>
<td>T-GDA-GRS</td>
<td>531.45</td>
<td>511.21</td>
<td>69.31</td>
</tr>
<tr>
<td>T-DA-GRS</td>
<td>446.13</td>
<td>419.37</td>
<td>44.23</td>
</tr>
</tbody>
</table>

applicable in practice. In all three aspects of cost functions, T-GDA-GRS yielded superior performances and hence it can be concluded that T-GDA-GRS is an improvement to T-DA-GRS. The interesting value of isolating_low_trusted_node in both types of networks emphasize the improvement of T-GDA-GRS over T-DA-GRS. While the T-GDA-GRS algorithm need only another 25% to reach the optimal value, the other algorithm has up to 50% to improve. Another interesting information lies in the optimal value crossing with isolating_low_trusted_node function from both table showing us that the optimal value cannot isolate all non-trustable node to terminal position, the value is not 100%. The loss number happens because of articulate node, the node in which removal can create a disconnected graph. In order to connecting through a network partition, the algorithms cannot isolate these articulate nodes to leaf of the tree. Hence, this articulate node can be seen as a point of failure in a partition which cannot be avoid in the assumption of this study. In static networks, more efficient trusted spanning trees in city street networks could be generated than in random networks. This is due to the fact that city street networks, in general, are more dense than random networks. In dynamic networks, density of the networks was not an important factor in determination of effective trusted spanning trees as dynamicity has more direct influence. A crucial factor which prevents maintaining efficient trusted spanning trees is that existing ones cannot be altered or modified unless break away of node(s) or merge(s) with other trees occur. This suggests that trusted spanning trees in a MANET may need to posses an ability to adapt and learn from their experience and local knowledge under the assumption that global knowledge cannot be assumed.

VII. CONCLUSION AND FUTURE WORK

As trust management in MANETs requires much attention recently due to its immense application and an active research area, management of DTM is even more problematic, and in turn, presents a greater challenge. While algorithms to manage trusted spanning trees proposed in this work may not be comprehensive and several other aspects are yet to be considered, they present a good starting point in trust management in DTM. This work affirms the advantage of greedy strategy and demonstrates its benefit in spanning trees traversal in such networks. Ability to assess and select effective spanning trees among many possibilities is crucial, this work proposes a method to assess them by means of three different cost functions. Their use may be beneficial in similar applications.

Future work can be carried out in several facets. T-DA-GRS and T-GDA-GRS merit further investigation. They can be tested on other types of network models. Good candidates of these are city traffic and city centre models as they may reveal some useful properties. As discussed in the previous section, an ideal trusted spanning tree is the one which can adapt itself for better efficiency. This suggests that the solution lies in invention of an adaptive trust management algorithm that is capable of learning from experience and local knowledge even under the assumption that global knowledge cannot be assumed because of dynamicity and decentralized nature of DTM.

REFERENCES